

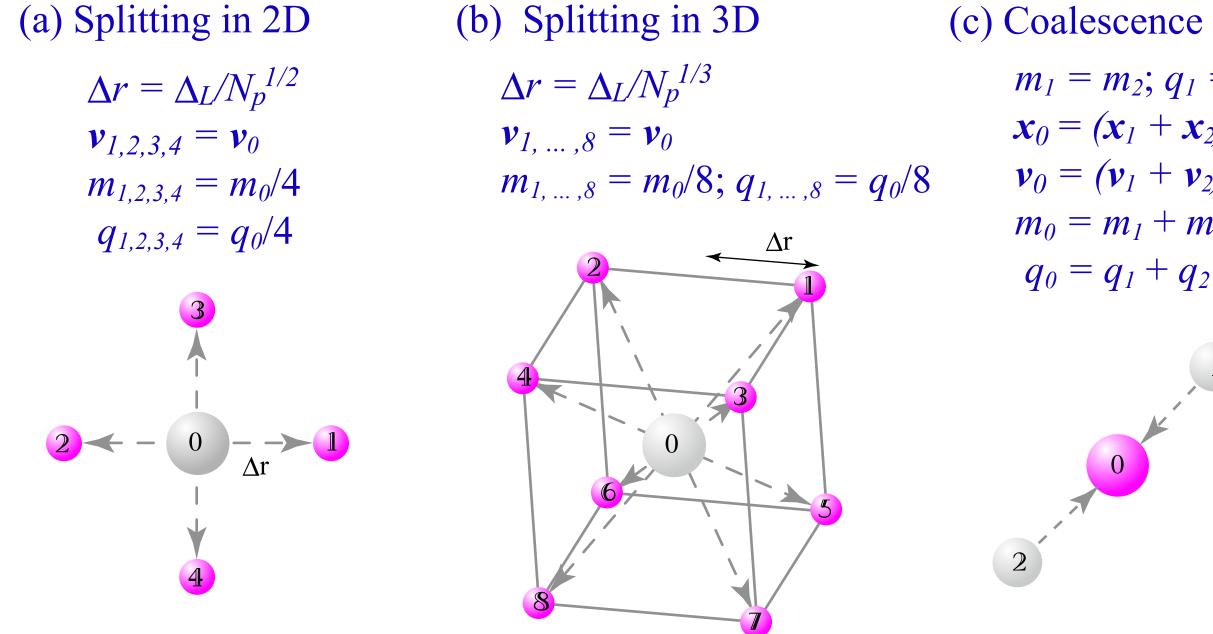
1. Introduction

Local kinetic processes in space and laboratory plasmas are, in many cases, considered to have a significant impact on global-scale energy transport and conversion processes. Magnetic reconnection is a typical case in which microscopic processes in the diffusion region, formed around the magnetic X-line, can control the MHD-scale dynamics. Generally, it is very difficult to describe in numerical approach such a phenomenon that includes a number of physical scales which can couple with each other.

The adaptive mesh refinement (AMR) technique is one of the promising methods to overcome the difficulties. It subdivides the computational cells locally in space and dynamically in time. In this study, we apply the AMR to the electromagnetic particlein-cell (EM-PIC) model for both the 2D and 3D systems, and successfully achieve efficient high-resolution simulations on the nonlinear evolution of the plasma sheet.

3. Particle Splitting & Coalescence

The number of particles per cell is controlled by splitting particles in fine cells and coalescing them in coarse cells.



4. Basic Equations

Particle Motions

$$\frac{\boldsymbol{v}^{n+1/2} - \boldsymbol{v}^{n-1/2}}{\Delta t} = \frac{q}{m} \left[\boldsymbol{E}^n(\boldsymbol{x}^n) + \frac{\boldsymbol{v}^{n+1/2} + \boldsymbol{v}^{n-1/2}}{2} \times \boldsymbol{B}^n(\boldsymbol{x}^n) \right]$$
$$\frac{\boldsymbol{x}^{n+1} - \boldsymbol{x}^n}{\Delta t} = \boldsymbol{v}^{n+1/2}$$

Electric & Magnetic Field

$$\begin{split} & \boldsymbol{E}_{L} = -\nabla \, \boldsymbol{\phi} \, ; \ \nabla^{2} \, \boldsymbol{\phi} = - \, \boldsymbol{\rho} \, / \, \boldsymbol{\varepsilon}_{0} \\ & \frac{\boldsymbol{E}_{T}^{n+1} - \boldsymbol{E}_{T}^{n}}{\Delta t} = c^{2} \nabla \times \frac{\boldsymbol{B}^{n+1} + \boldsymbol{B}^{n}}{2} - \boldsymbol{j}_{T}^{n+1/2} \, / \, \boldsymbol{\varepsilon}_{0} \, ; \ \boldsymbol{j}_{T}^{n+1/2} = \boldsymbol{j}^{n+1/2} + \boldsymbol{z}_{T}^{n+1/2} \\ & \frac{\boldsymbol{B}^{n+1} - \boldsymbol{B}^{n}}{\Delta t} = -\nabla \times \frac{\boldsymbol{E}_{T}^{n+1} + \boldsymbol{E}_{T}^{n}}{2} \\ & \boldsymbol{E}^{n+1} = \boldsymbol{E}_{L}^{n+1} + \boldsymbol{E}_{T}^{n+1} \end{split}$$

Electromagnetic Particle-In-Cell Model With Adaptive Mesh Refinement and Application to Magnetic Reconnection

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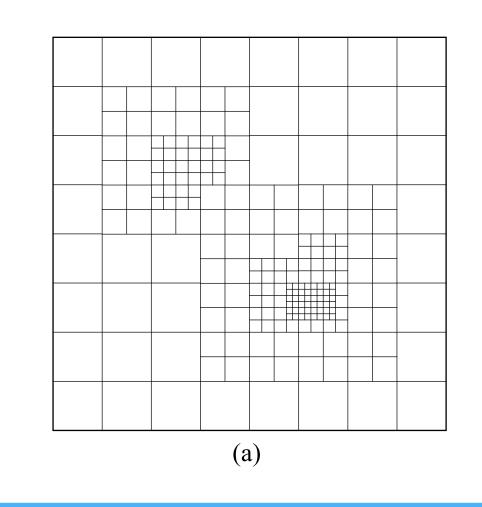
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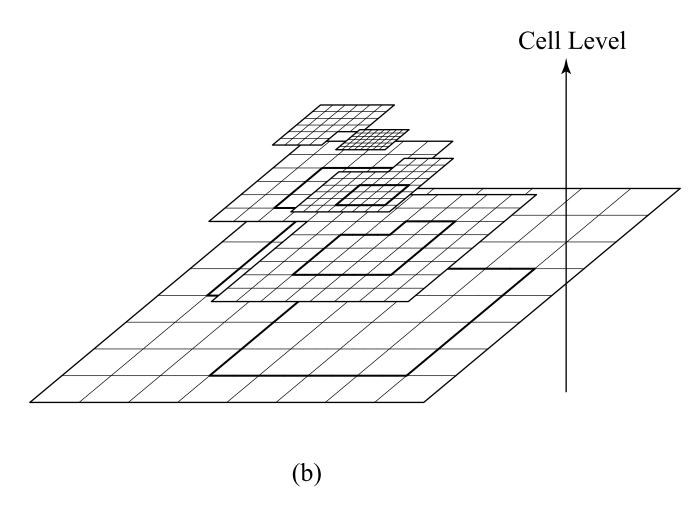
 $m_1 = m_2; q_1 = q_2$ $x_0 = (x_1 + x_2)/2$ $v_0 = (v_1 + v_2)/2$ $m_0 = m_1 + m_2$ $q_0 = q_1 + q_2$

$$- \varepsilon_0 rac{E_L^{n+1} - E_L^n}{\Delta t}$$

2. Data Structure

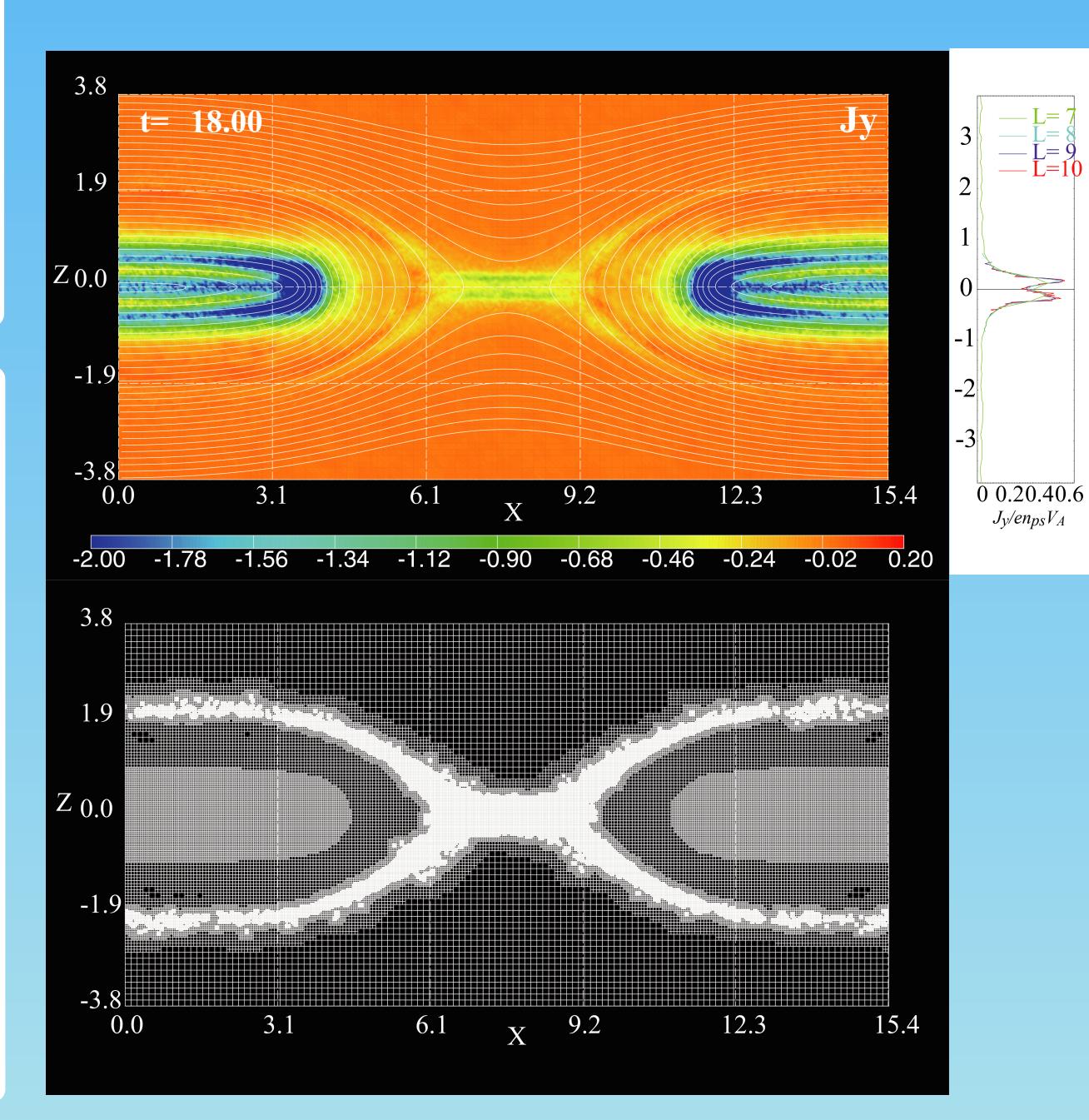
The AMR technique subdivides only cells that satisfy some refinement criteria and enhances the local spatial resolution. The data sets for the child cells are added onto the parent cell and develop a hierarchical tree structure.





5. Evolution of the Plasma Sheet

 $B_x(z) = -B_0 \tanh(z/\lambda)$; $n(z) = n_{ps} \operatorname{sech}^2(z/\lambda) + n_b \tanh^2(z/\lambda)$ $m_i/m_e = 100; T_{i,ps}/T_{e,ps} = 5.0; c/V_A = 20$ $\lambda = 0.5 \lambda_i; \quad n_b = 0.044 n_{ps}$



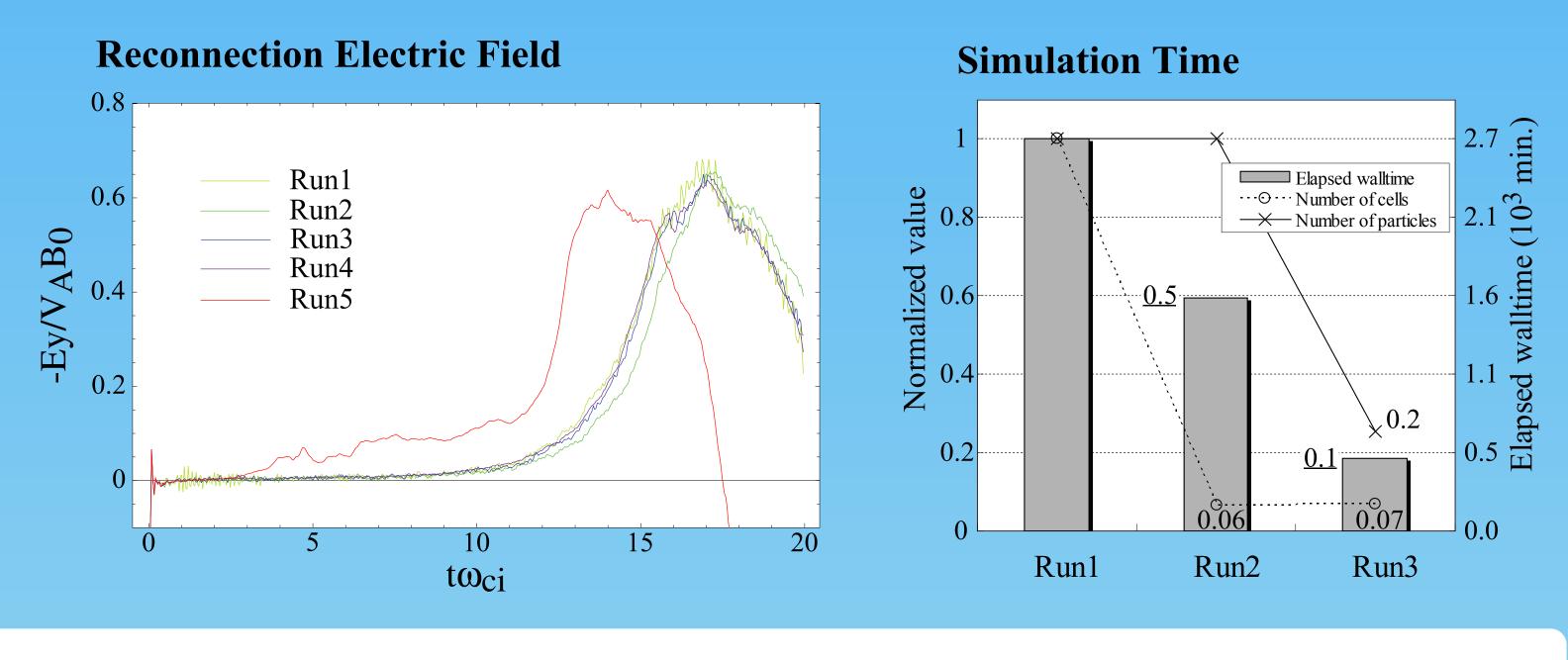
The hierarchical cell structure is supported by a set of pointers. Oct pointers

iPr (to parent cell)	Level
iNb (to parent cell of the neighboring Oct)	
inp (to a particle belonging to Oct)	Level
Cell pointers	
OctCh (to child Oct)	
Particle pointers	Partic
pNb (to a neighboring particle)	

Refinement Criteria $\Delta L > 2.0 \lambda_{De}$ or $V_{ev} > 2.0 V_A$

Simulation information

Run#	AMR	Particle splitting	System size	N _{ct}	N _{pt}
Run1	No	No	15.4 ×15.4	1.0×10^{6}	1.9×10^{7}
Run2	Yes	No	15.4×15.4	6.7×10^4	
Run3	Yes	Yes	15.4 ×15.4	7.1×10^4	
Run4	Yes	Yes	$15.4 \times 0.24 \times 15.4$	5.0×10^5	
Run5	Yes	Yes	15.4 ×1.92× 15.4	3.3×10^{6}	5.4×10^{8}

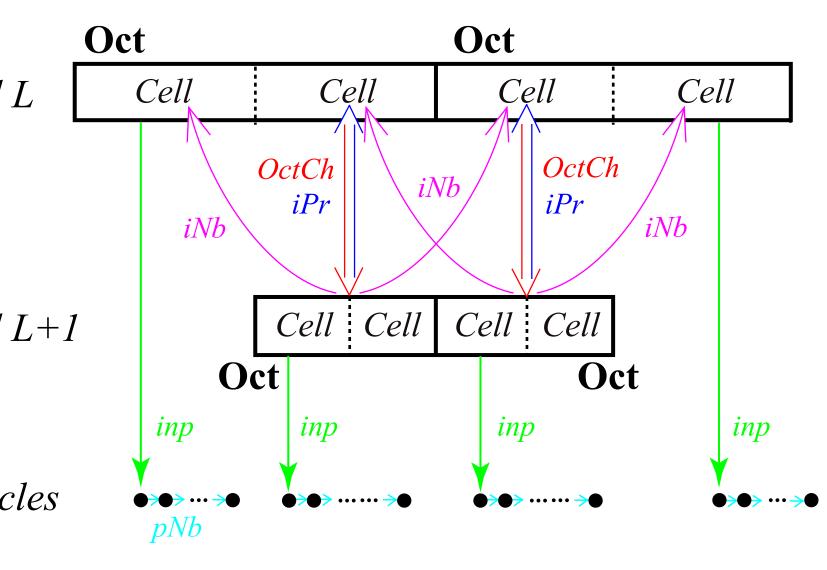


<u>6. Summary</u>

We have successfully developed a new EM-PIC code with the AMR both in the 2D and 3D systems. In order to control the number of particles per cell, the present code also performs the particle splitting and coalescence.

We have demonstrated that the AMR and particle splitting-coalescence techniques, combined with the EM-PIC code, enable efficient high-resolution simulations of the plasma sheet, and can be a promising method for studying physical phenomena which include a number of physical scales that can be coupled with each other.

Ref.	K. Fujimoto, and
	K. Fujimoto, and



S. Machida, J. Comput. Phys., 214 (2006) 550. R. Sydora, Comput. Phys. Comm., 178 (2008) 915.