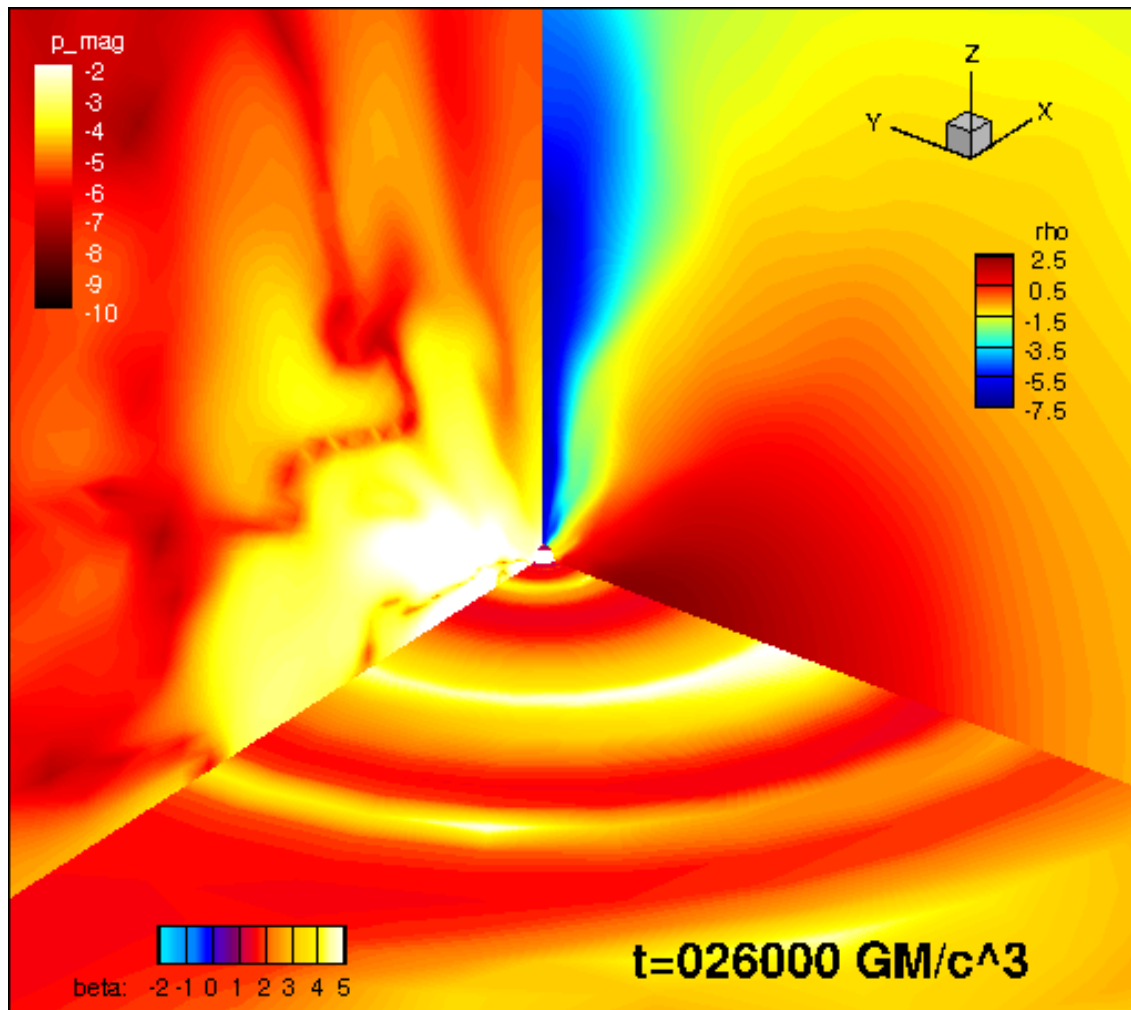


3D GRMHD simulations of accretion flows and relativistic jets

– for cosmic ray acceleration



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DTA Symposium

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Mizuta + in prep.

OUTLINE

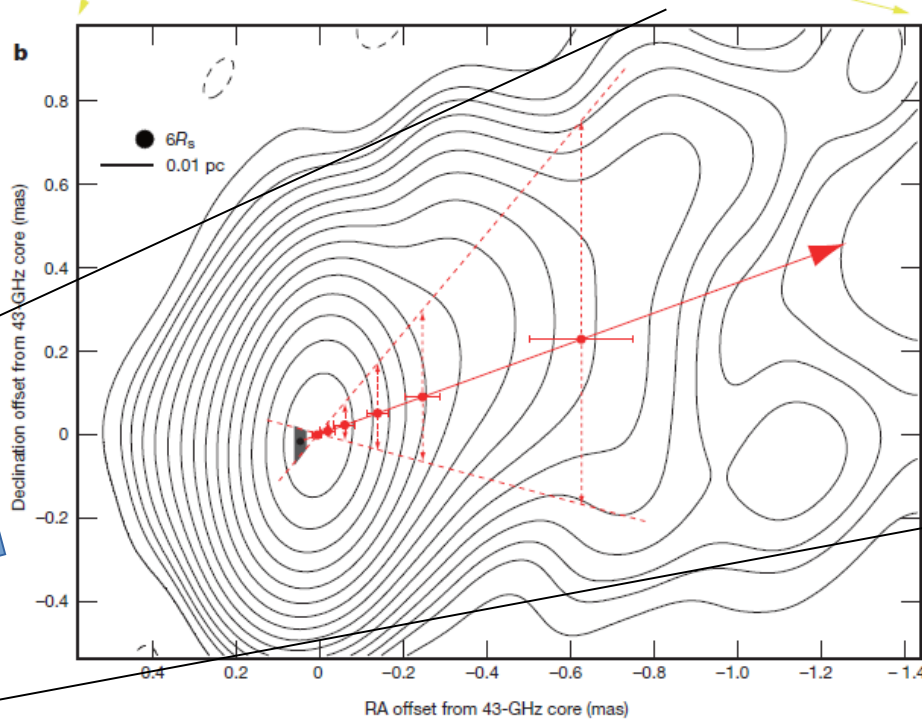
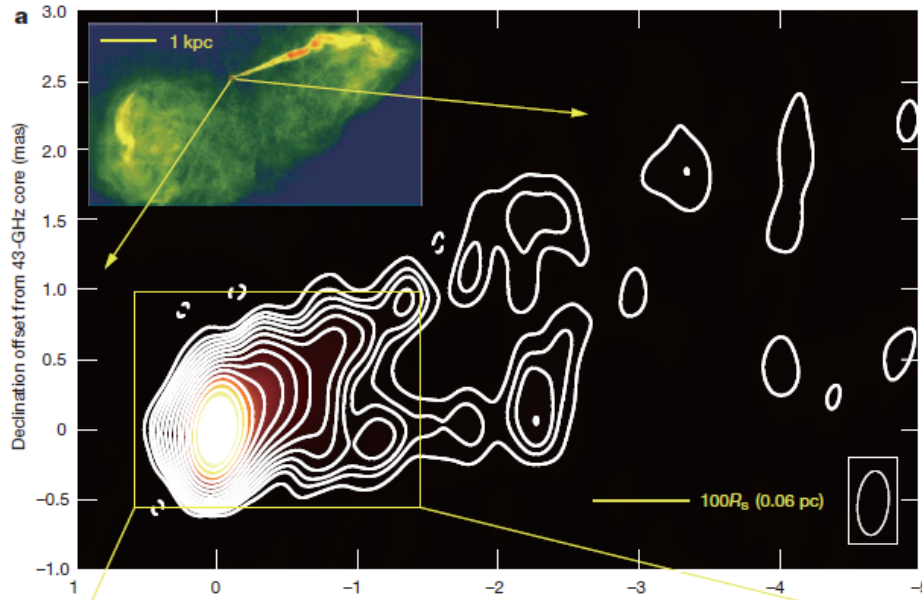
- Introduction
AGN jet
- GRMHD simulations of black hole and accretion disks
- Particle acceleration by wakefield acceleration for ultra high energy cosmic rays (<--> Fermi acceleration model)
- Summary

AGN and AGN Jets are laboratories for....

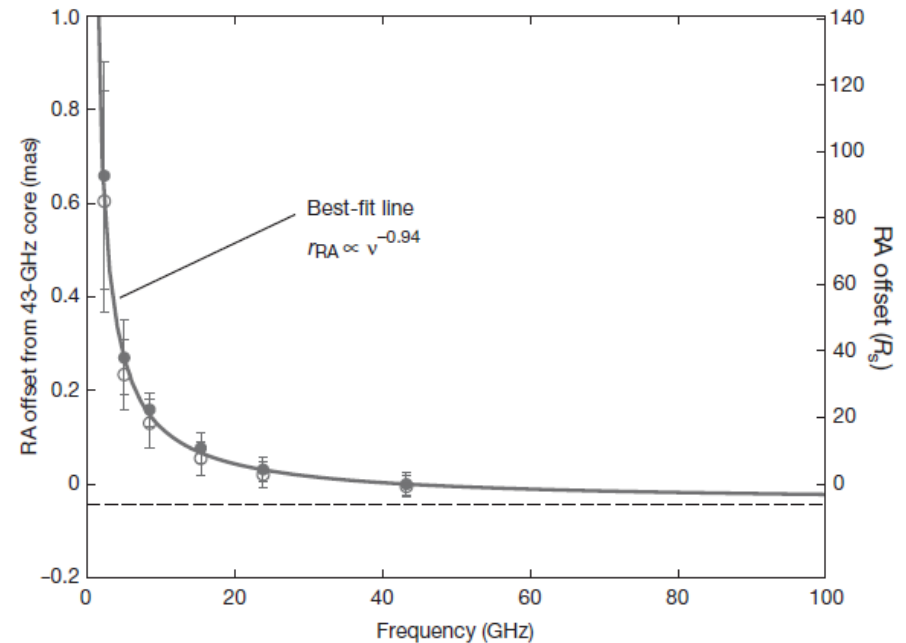
- Supermassive black hole $M \sim 10^6 - 10^{10} M_{\text{sun}}$
- Accretion disks
 - disk type & geometry (standard disk, ADAF, RIAF etc.)
 - angular momentum transport
(B-field amplification (Magnetorotational instability))
- jets
 - how to launch jets
 - how to collimate outflows and how to keep collimation
 - how to accelerate to relativistic bulk velocity ($\Gamma \sim 10$)
- high energy astrophysics
 - gamma-ray blazars (on-axis view, multiwavelength radio to high energy gamma-ray)
 - candidate object for particle accelerator of ultra-high energy cosmic rays

M87 radio observations

- M87 $D=16.7\text{Mpc}$
- $M_{\text{BH}} \sim 3.2\text{-}6.6 \times 10^9 M_{\text{sun}}$
- Location of the central BH is near the radio core by analysis of several bands of radio observations.
- It is consistent that the shape of the jet near the core is not conical but parabola.
- Rim brightening @ $100R_s$

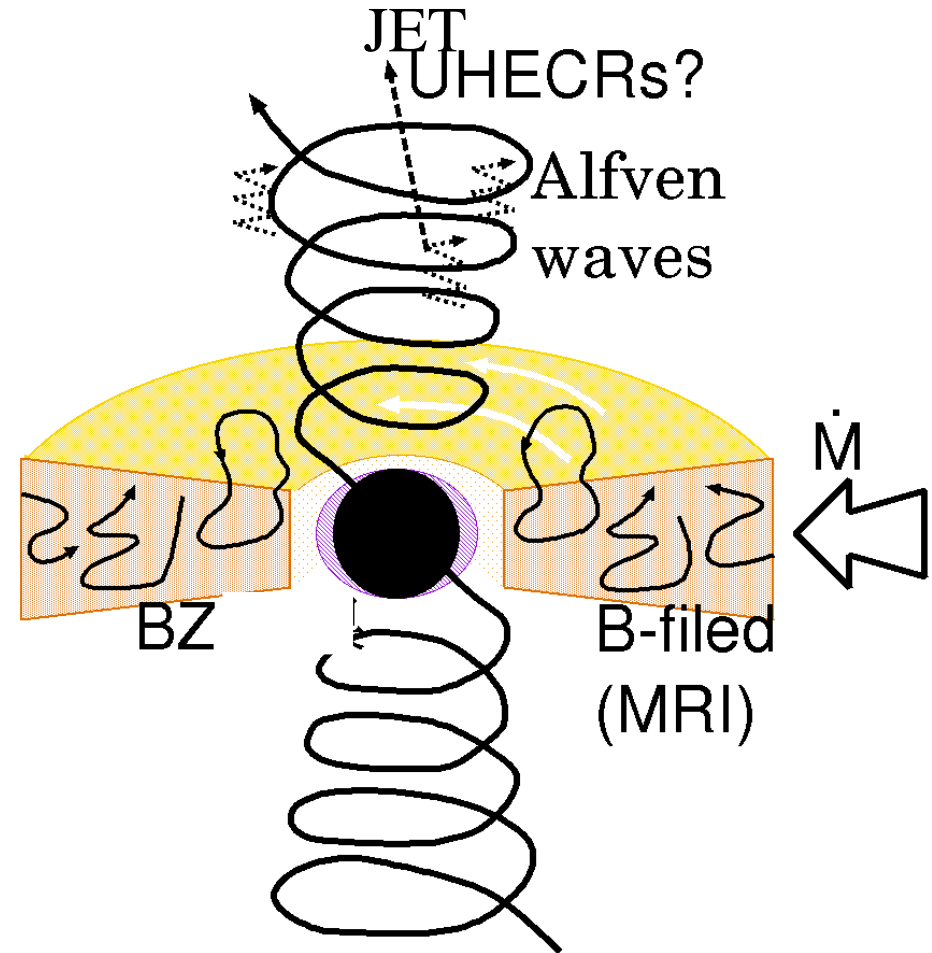
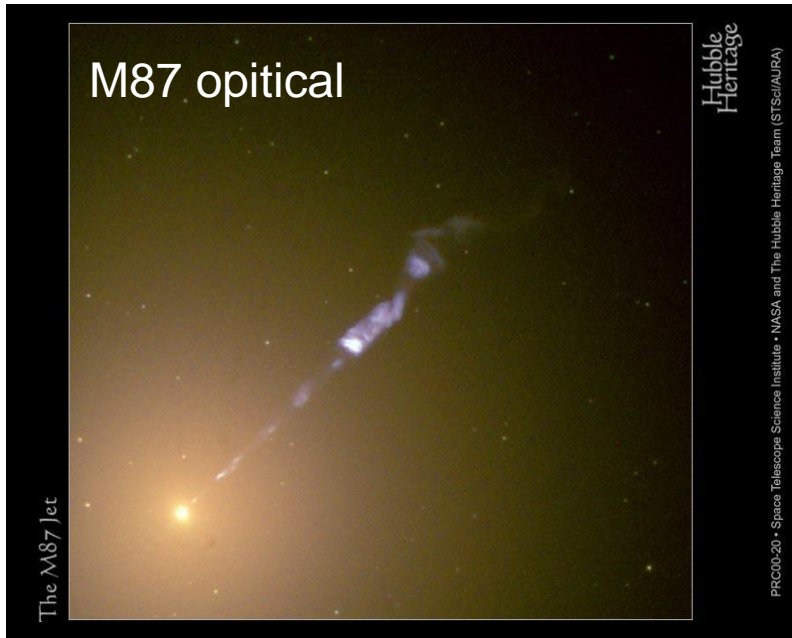


BH ?
No !



M87 radio observation Hada +(2011)

Relativistic jet launched from BH+accretion disk



- Central Engine
 - Black Hole(BH) + accretion disk
 - B filed amplification
- relativistic jet ($\Gamma \sim 10$ for AGN jet)
 - How to launch the jet is also a big problem for astrophysics.
 - Blandford-Payne (magnetic centrifugal force, B&P 1982)
 - Blandford-Znajek (general rela. + B filed effect, B&Z 1977)
 - or others ?

GRMHD simulations have been done in 2D & 3D (Koide+2002, McKinney, 2004, 2006 Komissarov+2005 2009, Nagataki 2009, Takahashi (2016) etc...

Basic Equations : GRMHD Eqs.

$GM=c=1$, a : dimensionless Kerr spin parameter

$$\frac{1}{\sqrt{-g}} \partial_\mu (\sqrt{-g} \rho u^\mu) = 0 \quad \text{Mass conservation Eq.}$$

$$\partial_\mu (\sqrt{-g} T_\nu^\mu) = \sqrt{-g} T_\lambda^\kappa \Gamma^\lambda_{\nu\kappa} \quad \text{Energy-momentum conservation Eq.}$$

$$\partial_t (\sqrt{-g} B^i) + \partial_j (\sqrt{-g} (b^i u^j - b^j u^i)) = 0 \quad \text{Induction Eq.}$$

$$p = (\gamma - 1) \rho \epsilon \quad \text{EOS } (\gamma=4/3)$$

Constraint equations.

$$\frac{1}{\sqrt{-g}} \partial_i (\sqrt{-g} B^i) = 0 \quad \text{No-monopoles constraint}$$

$$u_\mu b^\mu = 0 \quad \text{Ideal MHD condition}$$

$$u_\mu u^\mu = -1 \quad \text{Normalization of 4-velocity}$$

Energy-momentum tensor

$$T^{\mu\nu} = (\rho h + b^2) u^\mu u^\nu + (p_g + p_{\text{mag}}) g^{\mu\nu} - b^\mu b^\nu$$

$$p_{\text{mag}} = b^\mu b_\mu / 2 = b^2 / 2$$

$$b^\mu \equiv \epsilon^{\mu\nu\kappa\lambda} u_\nu F_{\lambda\kappa} / 2 \quad B^i = F^{*it}$$

GRMHD code (Nagataki 2009,2011)

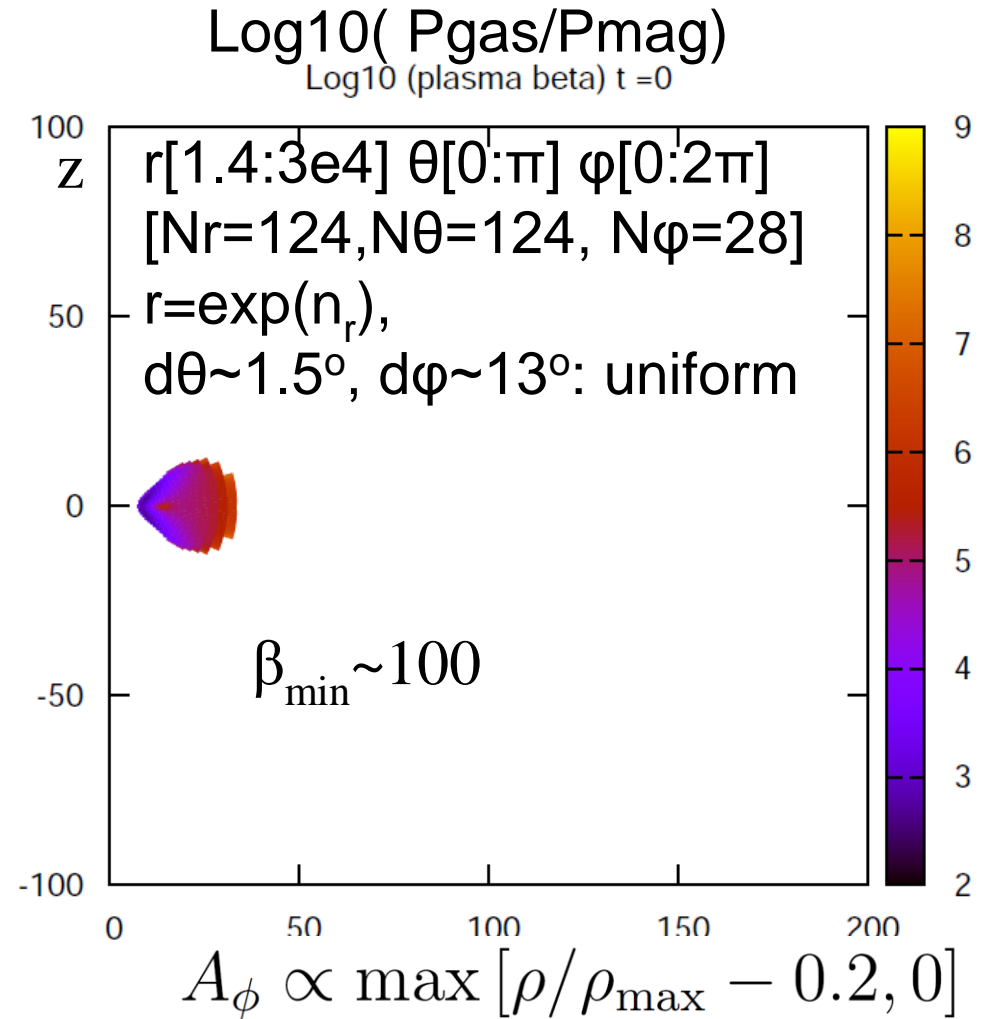
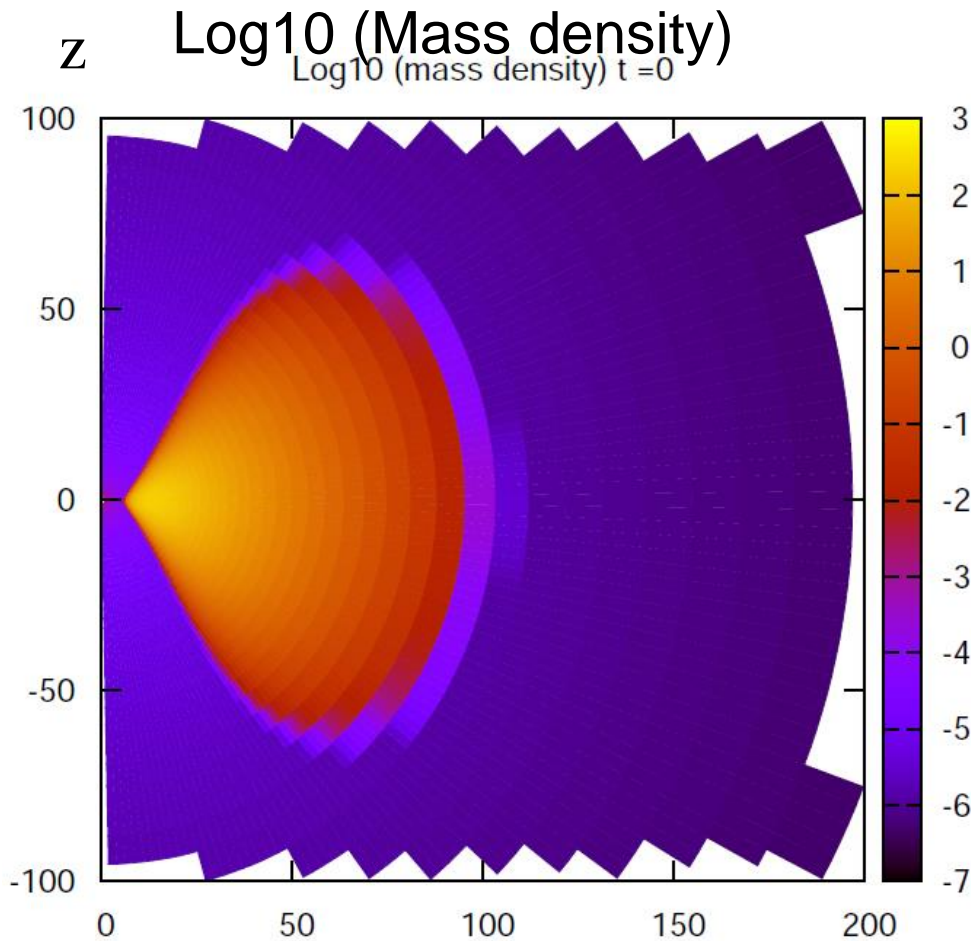
Kerr-Schild metric (no singular at event horizon)

HLL flux, 2nd order in space (van Leer), 2nd or 3rd order in time

See also, Gammie +03, Noble + 2006

Flux-interpolated CT method for divergence free

Initial Condition



Fisbone-Moncrief (1976) solution – hydrostatic solution of tori around rotating BH ($a=0.9$, $r_H \sim 1.44$), $l_* \equiv -u^t u_\phi = \text{const} = 4.45$, $r_{\text{in}} = 6. > r_{\text{ISCO}}$
With maximum 5% random perturbation in thermal pressure.

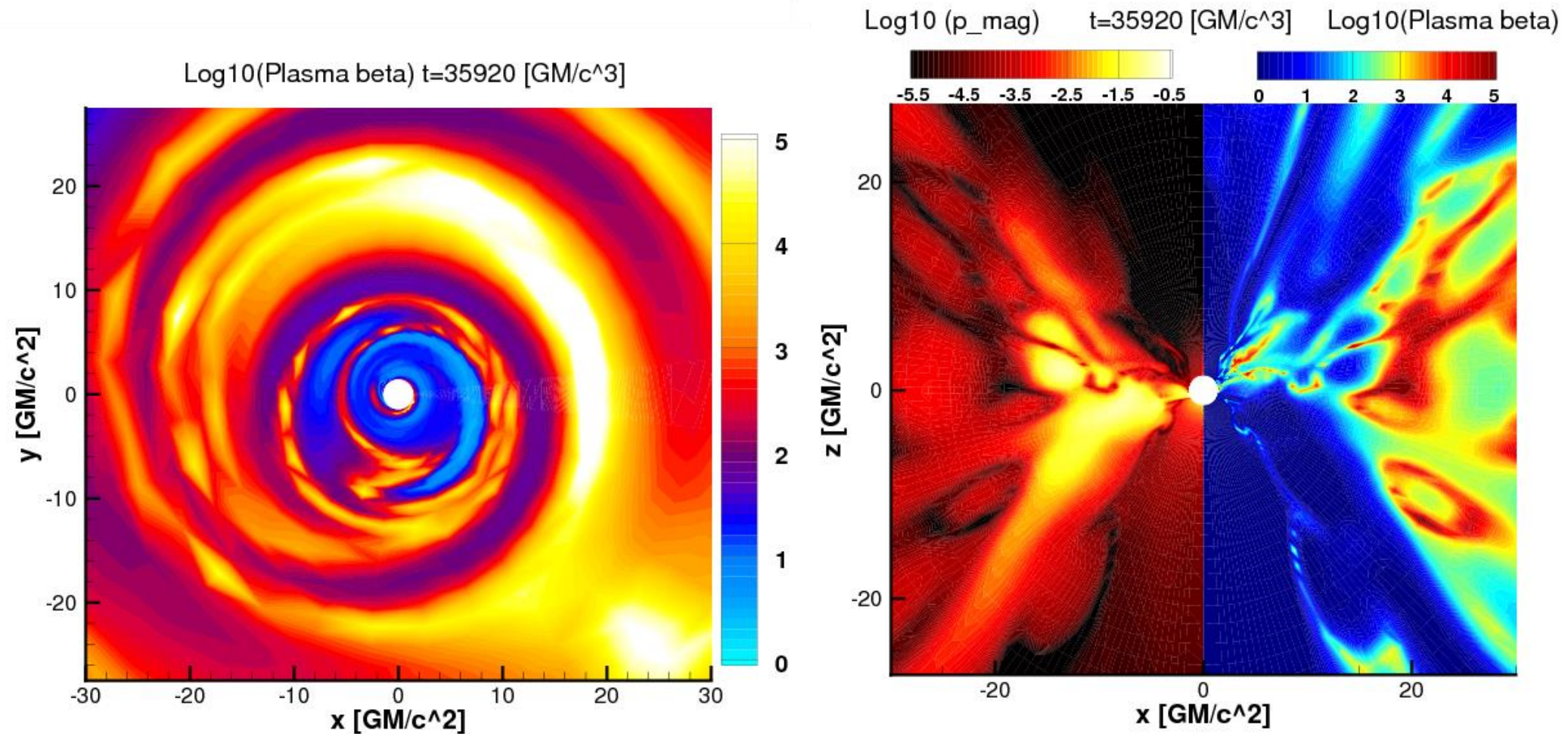
Units L : $R_g = GM/c^2$ ($=R_s/2$), T : $R_g/c = GM/c^3$, mass : scale free
 $\sim 1.5 \times 10^{13} \text{cm} (M_{\text{BH}}/10^8 M_{\text{sun}})$ $\sim 500 \text{s} (M_{\text{BH}}/10^8 M_{\text{sun}})$

Magnetized jet launch

movie

Low mass density and electromagnetic flux
along the polar axis. Intermittent

Plasma beta ($P_{\text{th}} / P_{\text{mag}}$) & magnetic pressure



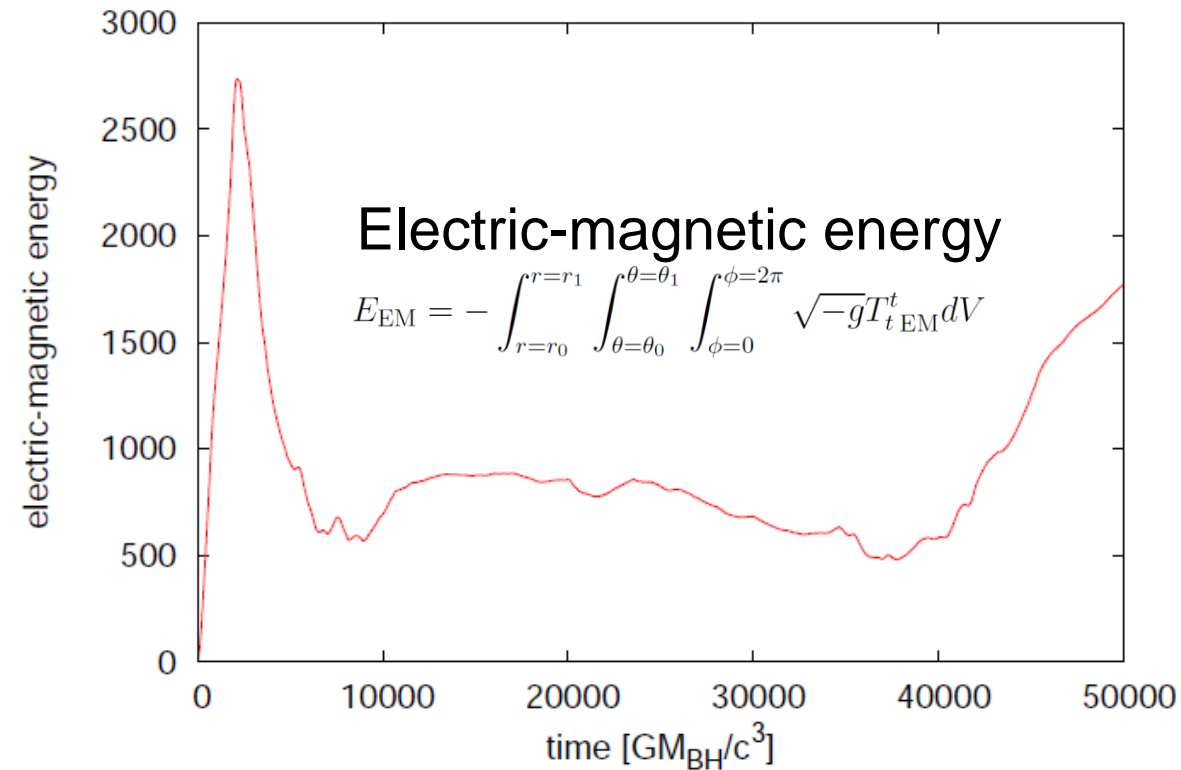
Plasma beta @ equator

Plasma beta (right)
Magnetic pressure (left)

Highly non-axis symmetric mode is excited.

Filamentary structure inside the disk with thickness $\sim 0.5 R_g$

Mizuta + in prep.

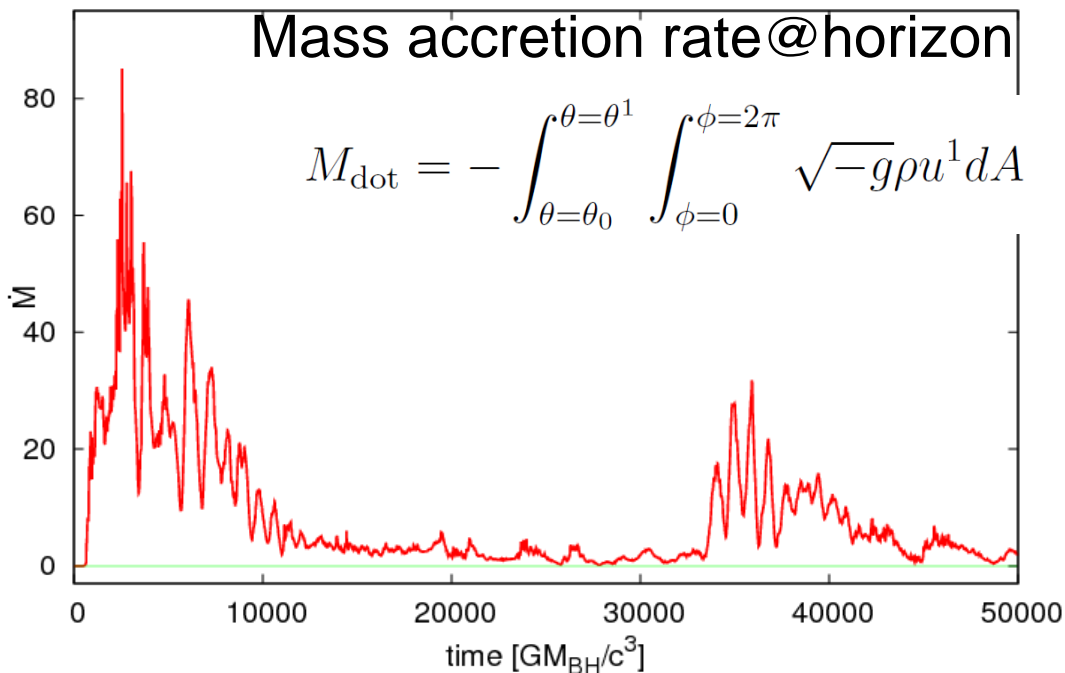


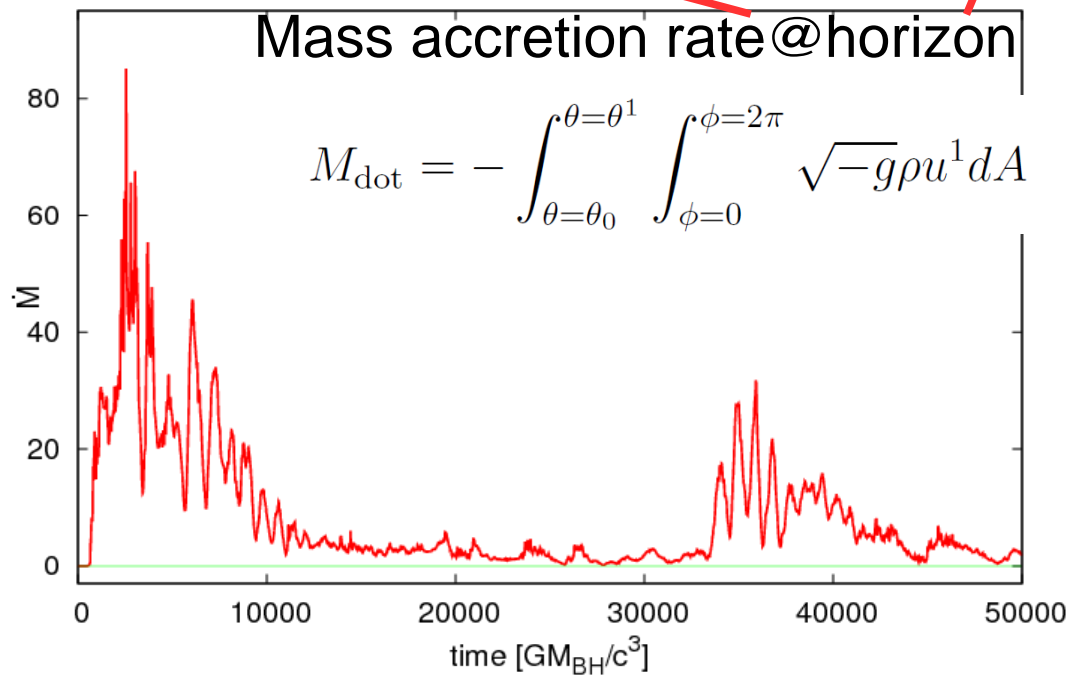
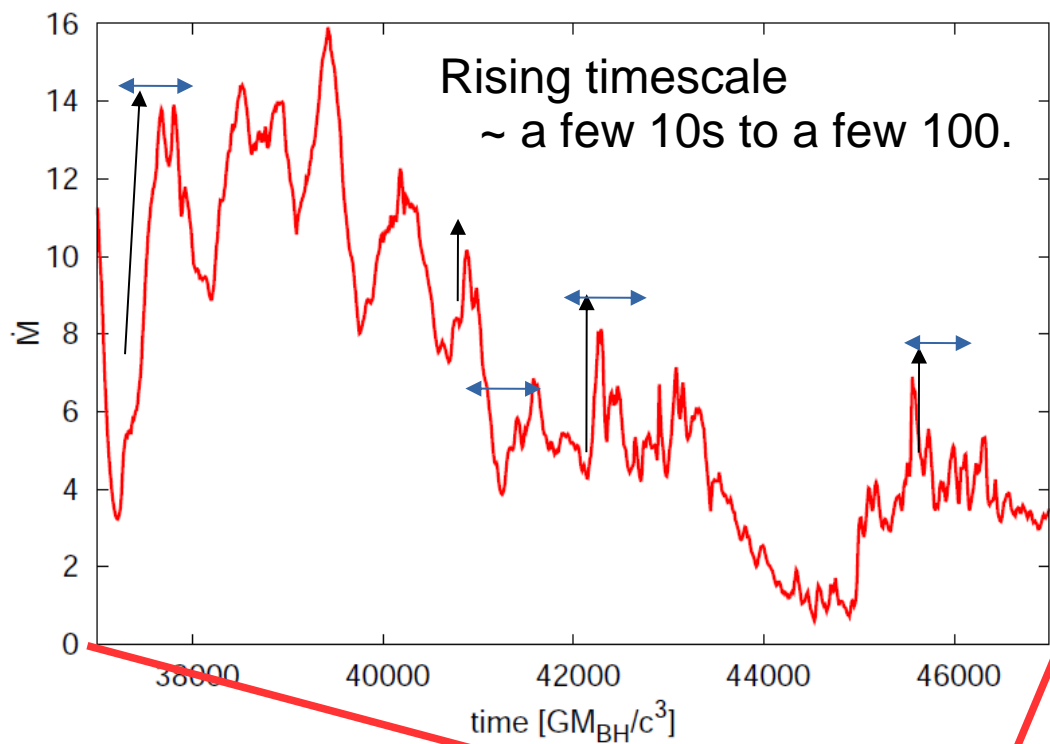
- B-field is well amplified.
- Mass accretion rate shows short time variability (~ a few tens) => consistent with MRI growth rate for $\lambda \sim 0.5 R_g$ ~8 grids size ~filamentary structure

- Recurrence rate ~ a few hundreds => consistent with high resolution local shearing box simulations. (high β state \leftrightarrow low β state)

$$\tau \sim 10 \Omega_K \sim 100 R_g/c$$

(Stone et al. 1996, Suzuki & Inutsuka 2009, O'Neill et al. 2011)





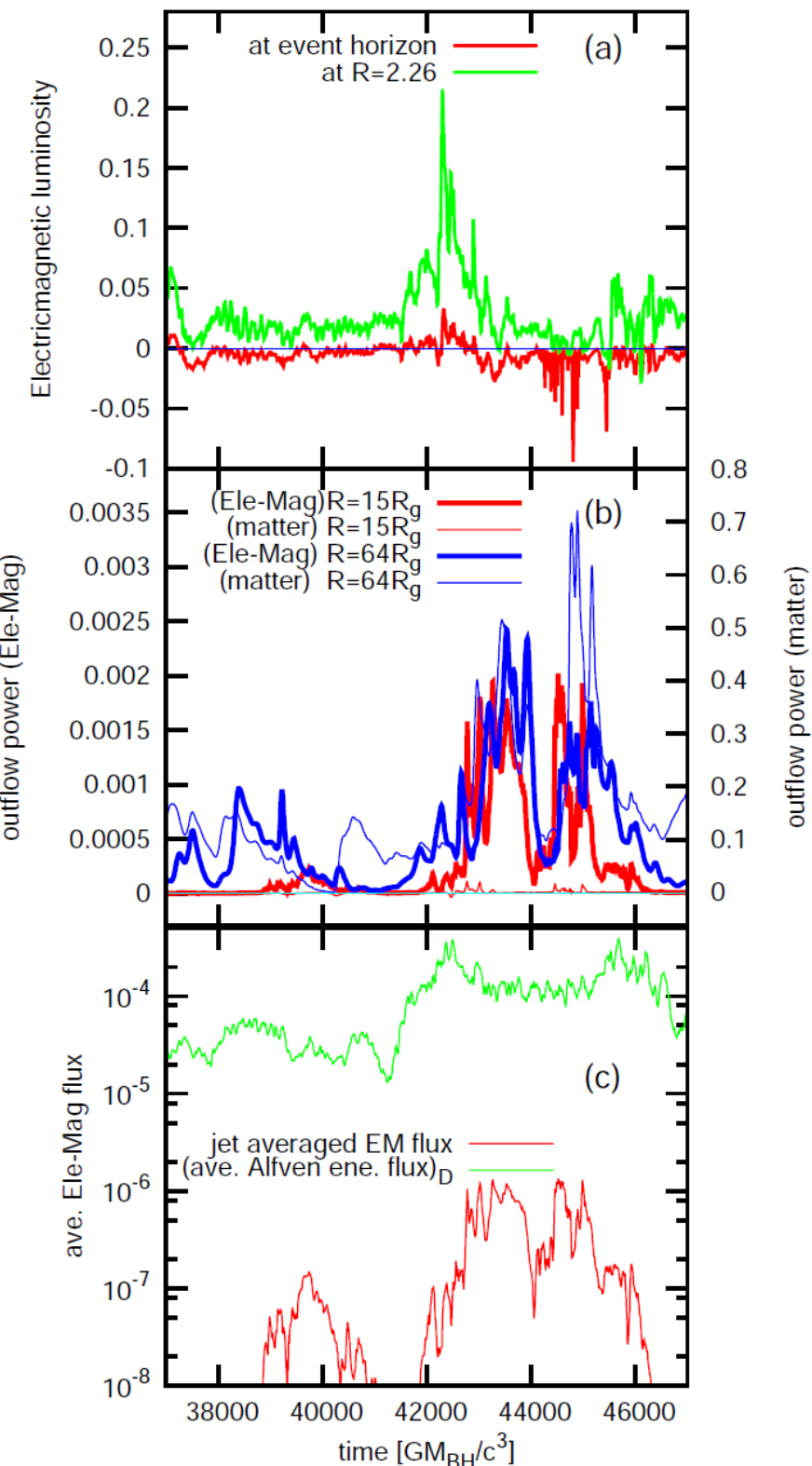
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- BZ-effect & outflow properties

Electric-magnetic luminosity @ horizon is sometimes positive.
 ==> BZ effect works.

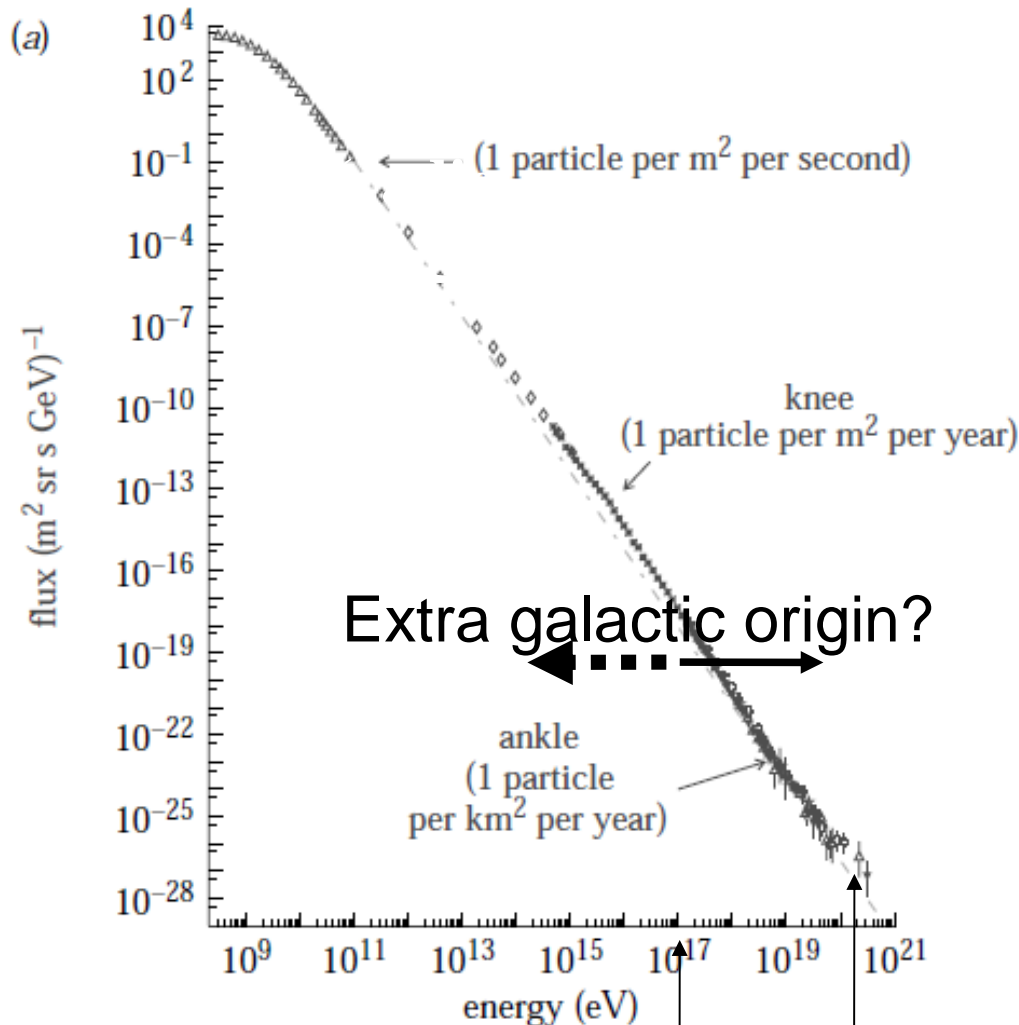
- But only ~1% in the jet

- Short time variability on electric-magnetic luminosity in the jet.
 This is similar with mass accretion rate.

- About 1% of poloidal component of the Alfven flux (disk) goes to the jet.

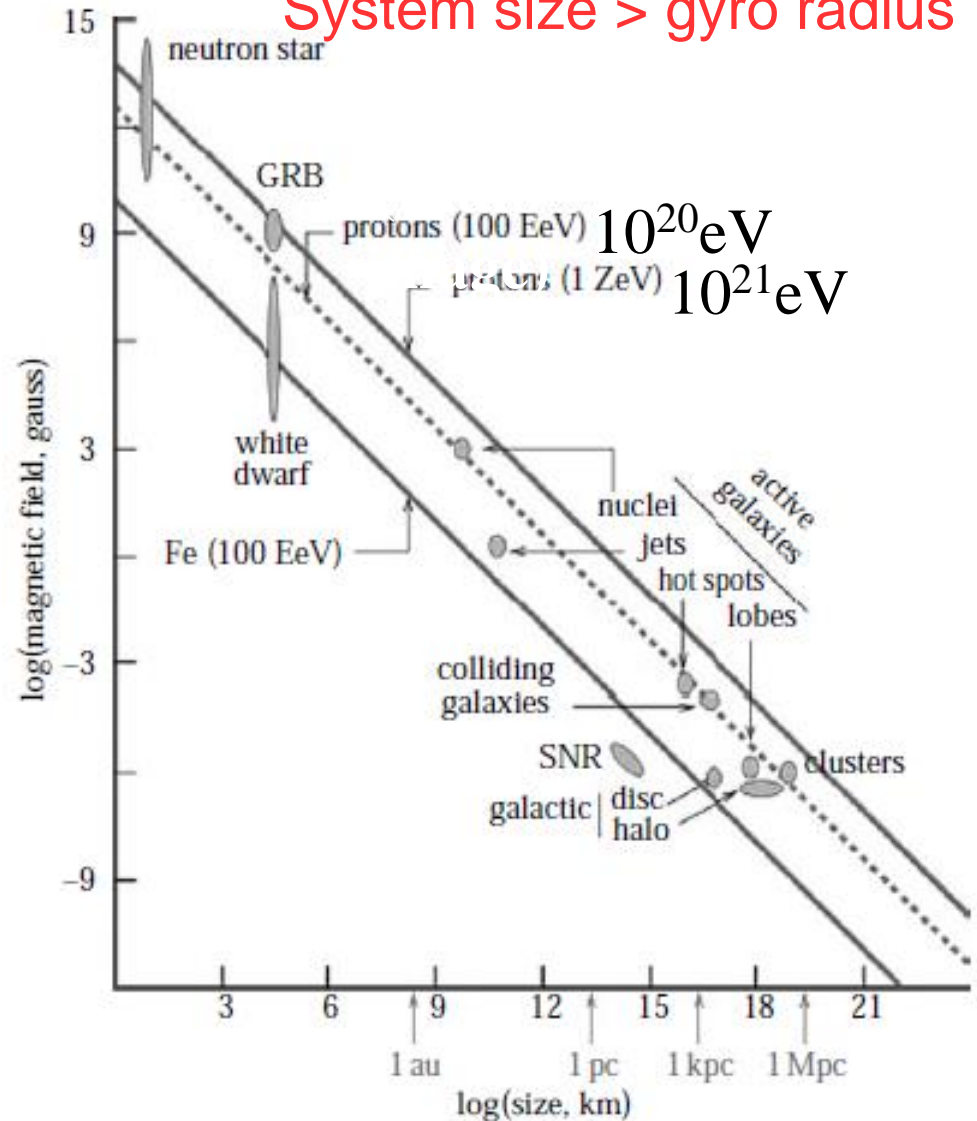
- Consistent with Ebisuzaki & Tajima model

Cosmic-ray up to $\sim 10^{20}$ eV



Hillas plot : $E_{\text{max}} \sim Z e B R$

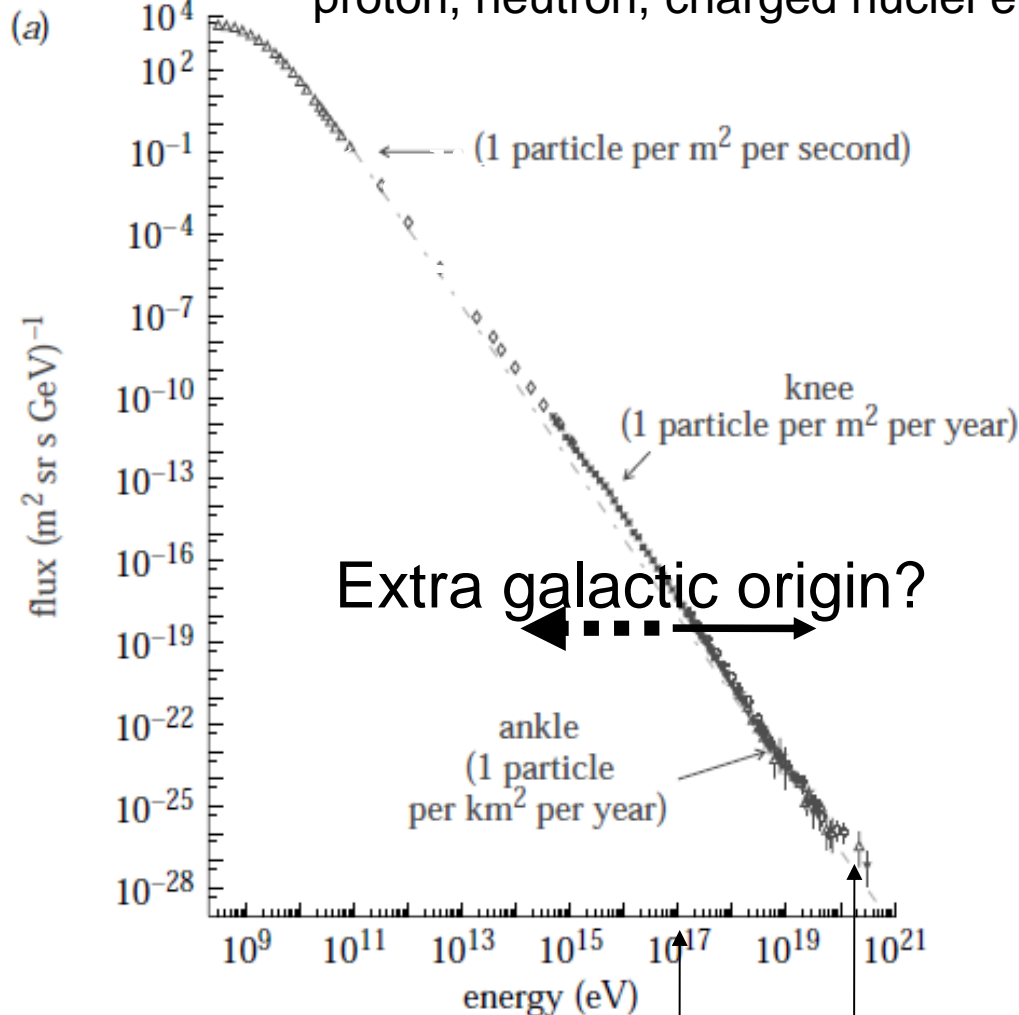
System size > gyro radius



LHC(14TeV Center-of-mass system)

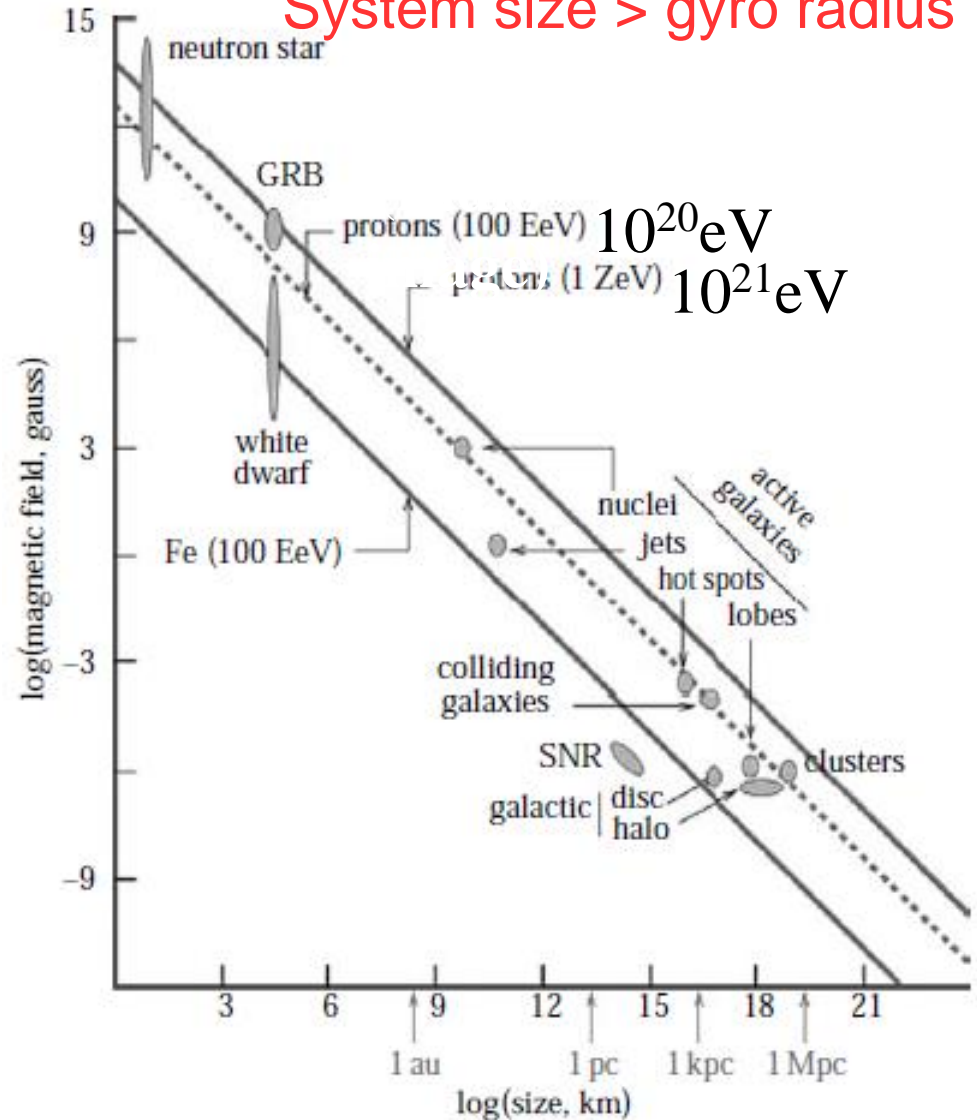
Cosmic-ray up to $\sim 10^{20}$ eV

Cosmic-ray- electron, positron, proton, neutron, charged nuclei etc.



Hillas plot : $E_{\text{max}} \sim Z e B R$

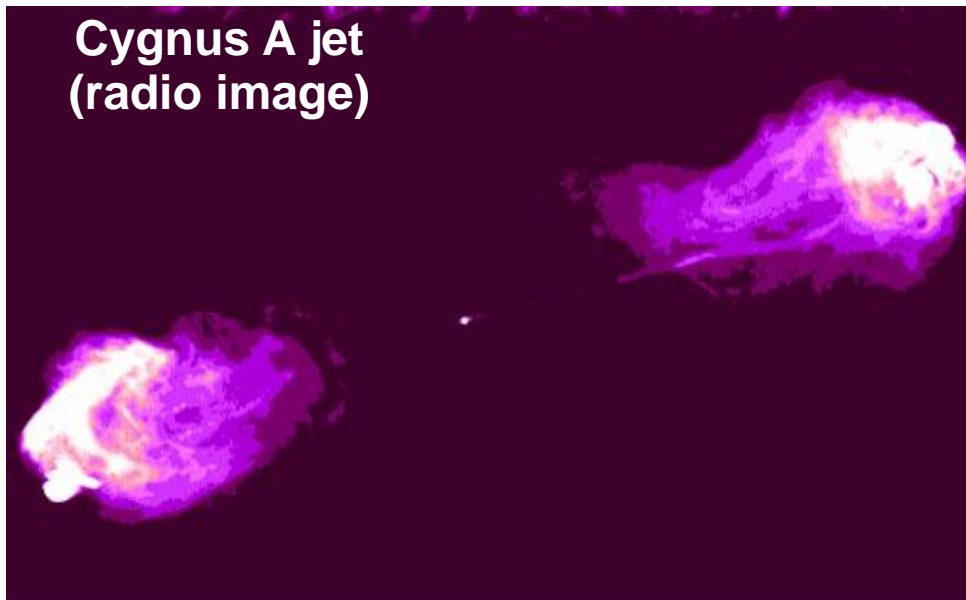
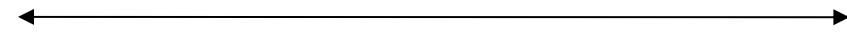
System size > gyro radius



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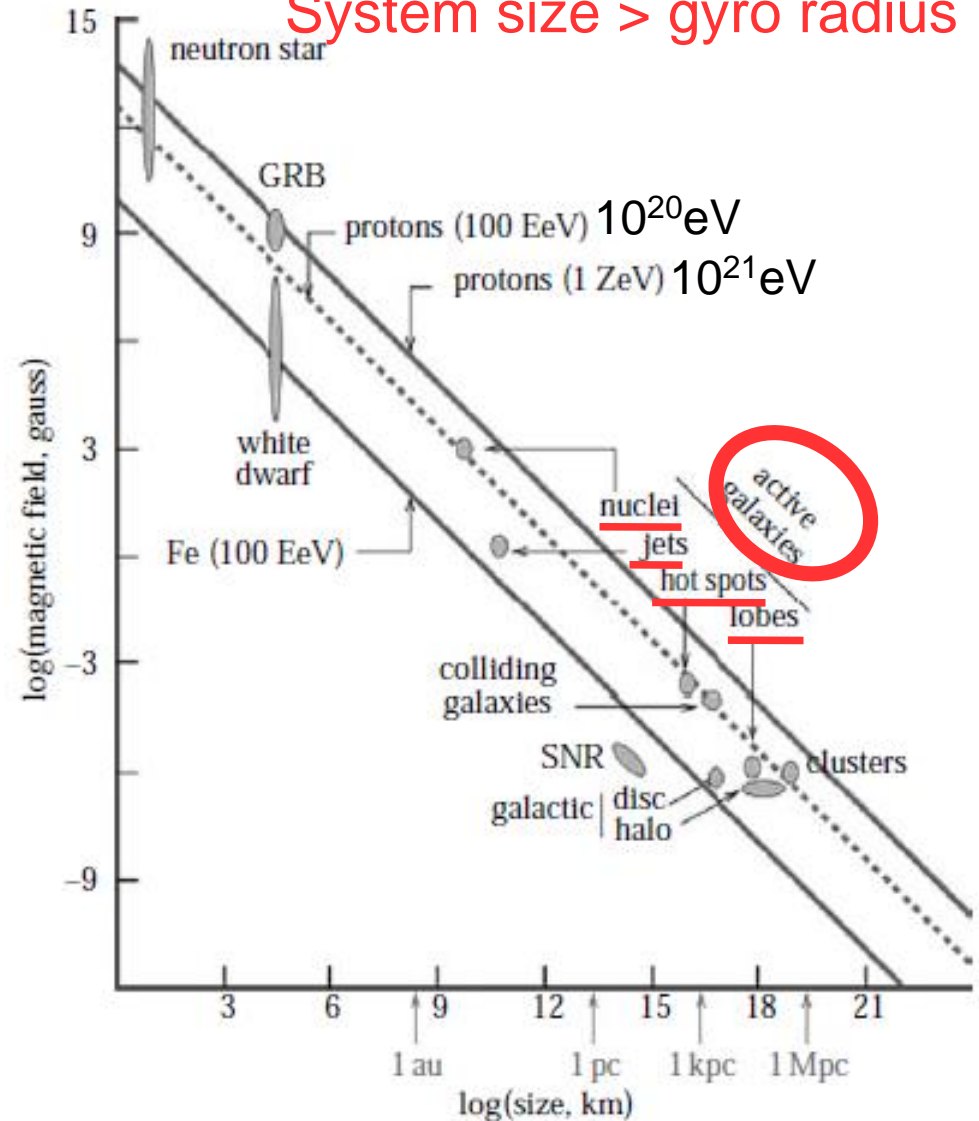
$\sim 10^{23}$ cm



Active galactic nuclei (AGN) jets are one of strong candidate objects for UHECR accelerator.

Hillas plot : $E_{\text{max}} \sim ZeBR$

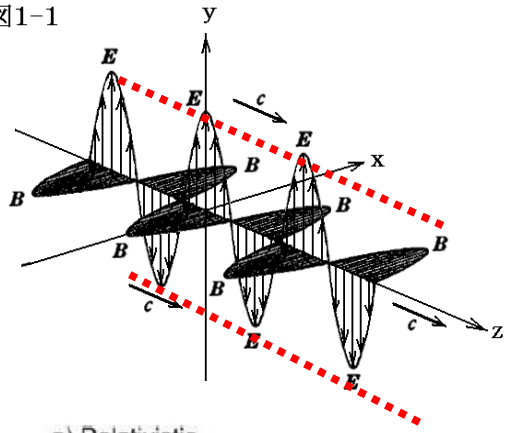
System size > gyro radius



Wakefield acceleration (Tajima & Dawson PRL 1979)

Acceleration mechanism by interaction between wave and plasma.

☒1-1



Laser plasma interaction
 \Rightarrow 8 shape motion.

$$\mathbf{F} = q \left(\mathbf{E} + \frac{\mathbf{v}}{c} \times \mathbf{B} \right)$$

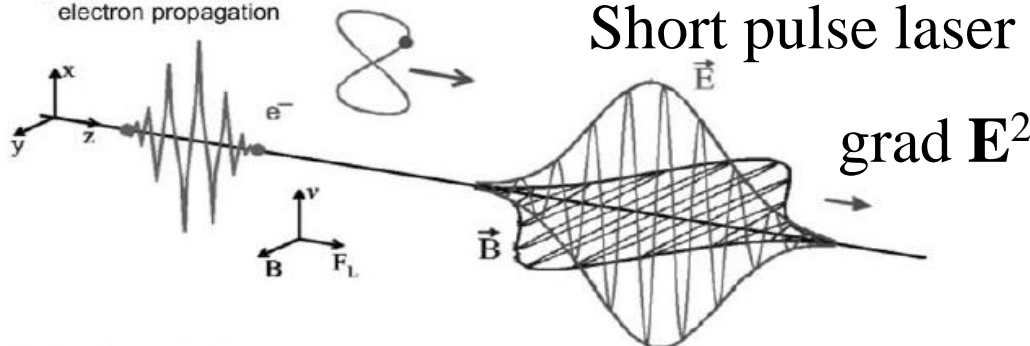
Oscillation by Electric field $\Rightarrow \mathbf{v}$
 (oscillation up, down)
 $\mathbf{v} \times \mathbf{B}$ force \Rightarrow oscillation forward
 and backward.

$|\mathbf{v}| \sim c \Rightarrow$ large amplification motion
 by $\mathbf{v} \times \mathbf{B}$. (8 shape motion).

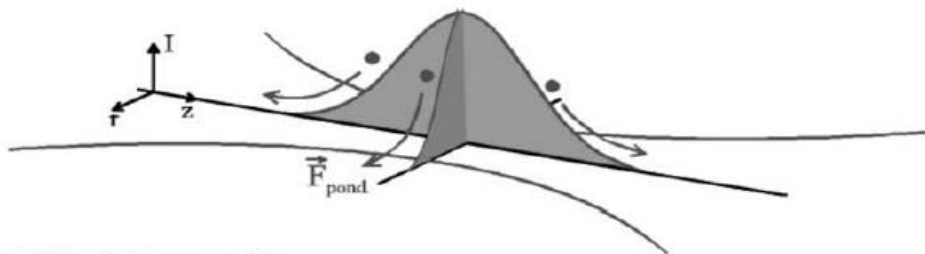
If there is gradient in E^2 , charged particles feel the force towards the E^2 side. = "Ponderomotive force"

Effective acceleration for
 $I \sim 10^{18} \text{ W/cm}^2$ (relativistic intensity).
 Experimentally observed.

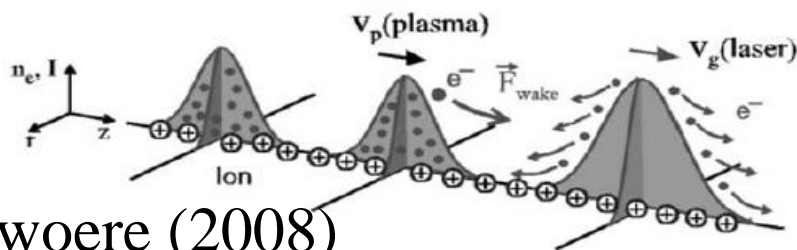
a) Relativistic electron propagation



b) Ponderomotive force



c) Wake field acceleration



Schwore (2008)

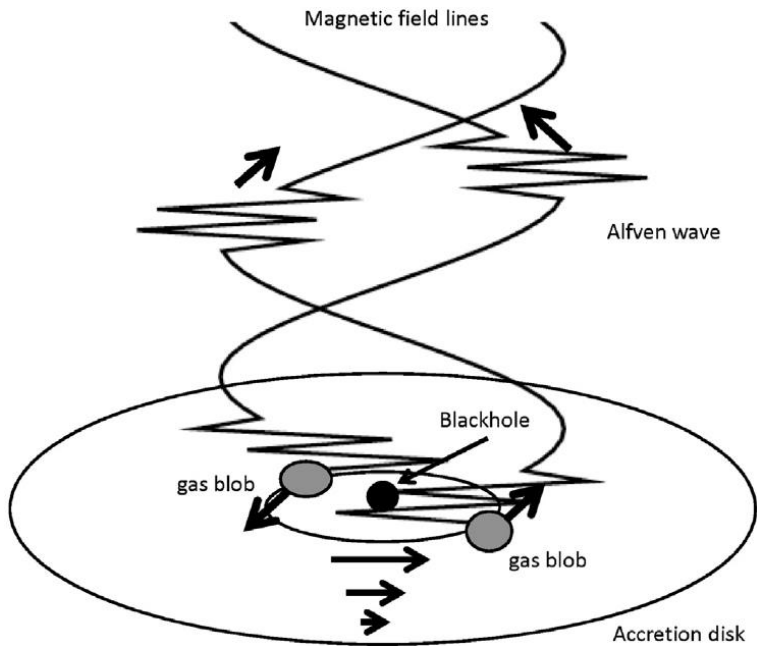
Relativistic Alfvén wave can be applied to wakefield acceleration. (Takahashi+2000, Chen+2002, Lyubarusky 2006, Hoshino 2008)

AGN : UHECR accelerator ?

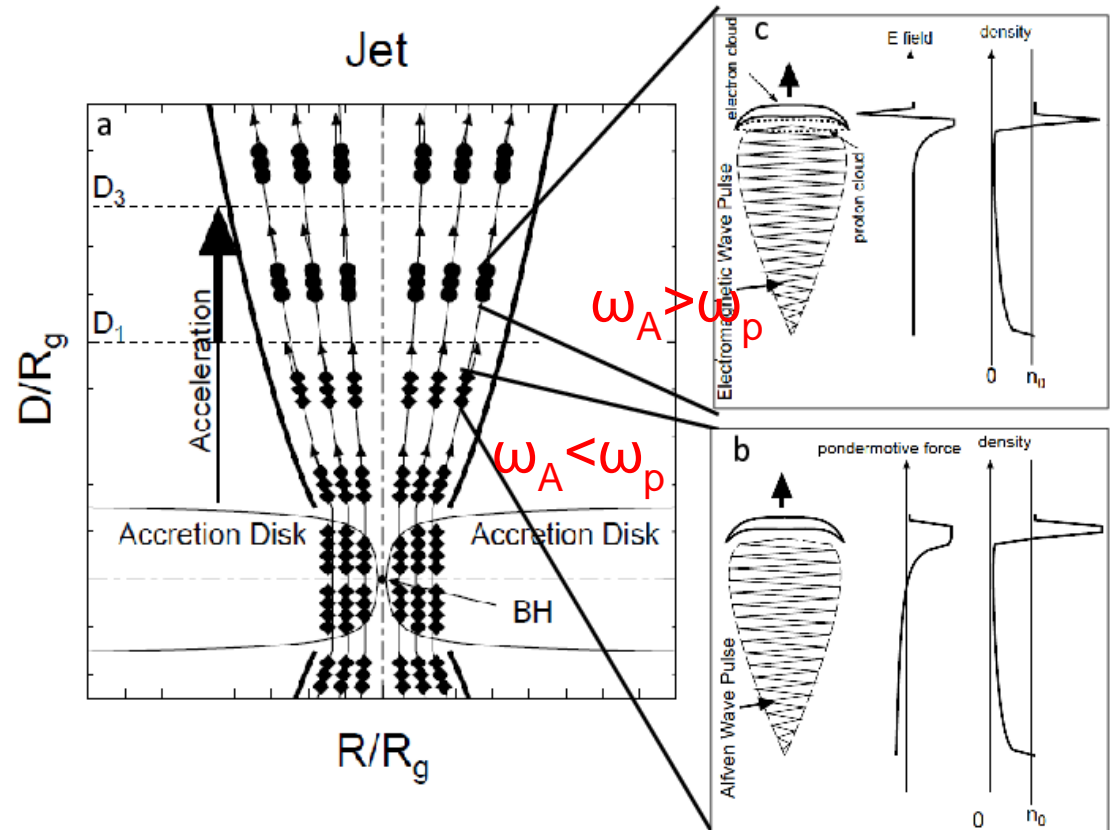
Wakefield acceleration model (excited by Alfvén wave) (Ebisuzaki & Tajima 2014)
 Relativistic Alfvén wave in the jet => electric-magnetic wave

$$a = \frac{eE}{m_e \omega_{AC}} = 2.3 \times 10^{10} \left(\frac{\dot{M}}{0.1 \dot{M}_c} \right) \left(\frac{M_{BH}}{10^8 M_\odot} \right) \gg 1$$

nonlinear & relativistic Alfvén mode for Standard-disk
 (Shakura & Sunyaev (1973) is assumed)



Ebisuzaki & Tajima 2014



Strength parameter a_0

In our numerical GRMHD simulation,

- So many electric magnetic flares are observed in the jet.
- Disk activities show MRI growth and eruption of Alfvén waves.

We can estimate the strength parameter a_0 as,

$$a_0 = \frac{eE}{m_e \omega_{AC}} = 7.6 \times 10^{12} \left(\frac{M}{10^8 M_\odot} \right)^{1/2} \left(\frac{\dot{M}_{av}}{10^{-2} L_{Ed}} \right)^{1/2}$$

Strength parameter highly exceeds unity.

The AGN jet can be good accelerator via wake-field acceleration.

Summary

3D GRMHD simulations of rotating BH+accretion disk for the analysis of wakefield acc.

- B field amplification
- Electromagnetic flux @ horizon (BZ effect)
- Electric magnetic flares in the jet
- consistent with Ebisuzaki & Tajima model
- $a_0 \sim 10^{12} \gg 1$: good accelerator for UHECRs via wakefield acceleration

Future works

- Higher resolution calculations are necessary to resolve fastest growing mode of MRI
- Different initial B-field topology